

# A routing framework for energy harvesting wireless nanosensor networks in the Terahertz Band

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**Abstract** Wireless NanoSensor Networks (WNSNs) will allow novel intelligent nanomaterial-based sensors, or nanosensors, to detect new types of events at the nanoscale in a distributed fashion over extended areas. Two main characteristics are expected to guide the design of WNSNs architectures and protocols, namely, their Terahertz Band wireless communication and their nanoscale energy harvesting process. In this paper, a routing framework for WNSNs is proposed to optimize the use of the harvested energy to guarantee the perpetual operation of the WNSN while, at the same time, increasing the overall network throughput. The proposed routing framework, which is based on a previously proposed medium access control protocol for the joint throughput and lifetime optimization

in WNSNs, uses a hierarchical cluster-based architecture that offloads the network operation complexity from the individual nanosensors towards the cluster heads, or nano-controllers. This framework is based on the evaluation of the probability of saving energy through a multi-hop transmission, the tuning of the transmission power of each nanosensor for throughput and hop distance optimization, and the selection of the next hop nanosensor on the basis of their available energy and current load. The performance of this framework is also numerically evaluated in terms of energy, capacity, and delay, and compared to that of the single-hop communication for the same WNSN scenario. The results show how the energy per bit consumption and the achievable throughput can be jointly maximized by exploiting the peculiarities of this networking paradigm.

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## 1 Introduction

Among the more promising research fields of today, nanotechnology is enabling the manipulation of matter at an atomic and molecular scale, from one to a hundred nanometers. One of the goals of nanotechnology is to engineer functional systems based on the unique phenomena and properties of matter at the nanoscale [5]. Currently, a great research effort is spent in the attempt to realize nanoscale machines, also called molecular machines or nanomachines, defined by Drexel [6] as “mechanical devices that perform useful functions using components of nanometer-scale and defined molecular structure”. More specifically, nanosensors [1] are nanomachines expected to have the ability to sense, compute, manage their energy,

and interconnect into networks, termed Wireless Nano-Sensor Networks (WNSNs), to overcome their individual limitations and benefit from collaborative efforts. WNSNs will take advantage of novel nanomaterial-based sensing processes to detect new types of events at the nanoscale, and they are expected to enable advanced applications of nanotechnology in the biomedical field (e.g., intrabody health monitoring and drug delivery systems), environmental control (e.g., agriculture plague and air pollution control), and defense and military technology (e.g., surveillance against new types of biological and chemical attacks at the nanoscale).

Among the many peculiarities of nanosensors, two main characteristics, combined with their limited computational resources [14], are expected to guide the design of WNSNs architectures and protocols, namely, their wireless communication technology and their energy harvesting process. The limited size of nanosensors is notoriously excluding the possibility of designing on-board classical antennas, which would radiate only at extraordinary high frequencies, up to hundreds of THz, infeasible given the limited energy resources available. Nanomaterial-based antennas, in particular graphene-based antennas [10, 11, 16, 17] and nano-transceivers [4, 11, 15], are proposed as a solution to the aforementioned problem, since the properties of graphene allow them to radiate in the Terahertz Band, within 0.1 and 10 THz, while having a form factor suitable to be integrated into nanosensors. Very high propagation losses and a very large available bandwidth are the main Terahertz Band communication characteristics [8, 13] which have to be taken into account to develop efficient WNSNs architectures and protocols, while jointly taking into account the limited nanosensor resources in terms of computational power and energy.

An energy harvesting process is required by nanosensors to cope with the limited size and flexibility of their energy storage, which is realized by means of nano-batteries. In this direction, energy harvesting processes at the nanoscale have been recently proposed [3, 7, 19], which convert several different forms of energy, e.g., vibrational, fluidic, electromagnetic, or acoustic, into electrical energy. The peculiarities of these nanoscale energy harvesting processes combined with the limited energy storage of the nanosensors result in temporal fluctuations of the available energy of each nanosensor, which have to be taken into account when designing WNSNs architectures and protocols. In this direction, WNSNs have the potential to achieve an infinite lifetime and perpetual operations if carefully adapted to these peculiarities, as detailed in [18].

The very high density of nodes expected for a WNSNs, combined with the very high propagation losses of the Terahertz Band channel and the need to efficiently meet the conditions for perpetual network operations, require the

development of novel routing protocols for multi-hop communication in WNSNs. To the best of our knowledge, there are no routing protocols for WNSNs. In addition, previous work on energy efficient routing in WSNs is not directly applicable to WNSNs, since the peculiarities of the Terahertz Band communication [8], in particular the very unique distance-dependent behavior of the available bandwidth and the power control techniques that can be employed to reach the optimal transmission rate, are not taken into account. Moreover, other work focused on routing in WSN with energy harvesting nodes does not capture the particular characteristics of the energy harvesting processes at the nanoscale [9], in particular the collection of vibrational energy through piezoelectric nanogenerators. As a consequence, novel solutions for the design of a routing scheme, where the peculiarities of the wireless communication in a WNSN are combined with the energy-efficient management of the information routing scheme, are needed.

In this paper, we devise a novel routing framework based on the peculiarities of the WNSNs, both in term of Terahertz Band communication and nano-scale energy harvesting. First, this routing framework is based on a hierarchical cluster-based architecture where the WNSN is partitioned into clusters. Within each cluster, a nano-controller, which is a nano device with more advanced capabilities than a nanosensor, coordinates the nanosensors and gathers the data they communicate [1]. This hierarchical cluster-based architecture is specifically devised to manage most of the complexity of any network protocol or algorithm at the nano-controller, and to cope with the limited resources of the nanosensors. Moreover, since the communication within the nanosensor network involves high-bit-rate transmissions in the Terahertz Band, the nano-controller is also responsible to guarantee the necessary synchronization at the physical layer. To reach this objective, our routing framework stems from the MAC protocol recently proposed in [18], where a joint throughput and lifetime scheduling is performed by the nano-controller on top of a Time Division Multiple Access TDMA framework within each cluster. In our routing framework, we specialize this throughput and lifetime scheduling to the multi-hop case, where a joint management of the direct communication from the nanosensors to the nano-controller and the multi-hop communication among nanosensors is performed, as detailed in Sect. 2.2

Second, our routing framework is based on the evaluation of the probability of saving energy by initiating a multi-hop communication route from a source nanosensor compared to a direct transmission from the source nanosensor to the nano-controller. This evaluation is executed at the nano-controller, which is expected to make a decision toward multi-hop or direct communication on the basis of

the probability value. This procedure allows to initiate a multi-hop communication only when there is a sufficient probability of saving energy, which would finally result in an increase of the overall throughput of the network, as explained in Sect. 2.3

Third, in case of multi-hop communication, the nano-controller is expected to optimize the distance of the next hop through a control on the transmission power of the source nanosensor. This transmission power is adapted to the Critical Neighbor Range (CNR) parameter, defined in Sect. 2.4 as the optimal distance at which the next hop should be located from the source nanosensor to achieve the best trade-off between the throughput and the distance from the receiving neighbor node that guarantees a pre-defined received SNR value, while at the same time satisfying the condition for infinite network lifetime.

Finally, the selection of the next hop is operated in a distributed fashion, where each nanosensor sets its likelihood to be elected as next hop depending on the load in its retransmission buffer, the level of its stored energy, its closeness to the CNR, and its relative location with respect to the source nanosensor and the nano-controller, as detailed in Sect. 2.5 This procedure allows a balance in the use of the energy and computational resources in each cluster of the WNSN, while allowing the optimization of the throughput and guaranteeing the perpetual operation of the network.

The rest of the paper is organized as follows. The proposed routing framework is detailed in Sect. 2 Numerical results are included in Sect. 3, where a performance evaluation is conducted through simulations by comparing the proposed routing framework with a more basic single-hop communication. Finally, in Sect. 4 we conclude the paper.

## 2 WNSN routing framework

The objective of the routing framework is to provide the nanosensor network with a procedure to save the average energy harvested from the environment by the nanosensors and increase the overall throughput in the transmission of information from the nanosensors to the nano-controller. The routing decision framework is built on top of the Medium Access Control (MAC) protocol introduced in our previous work in [18], where a throughput-and-lifetime optimal scheduling was designed to manage a variable-length time slot assignment to the nanosensor for their direct transmission of information to the nano-controller. In this paper, we enhance this protocol by introducing the capability for each nanosensor to relay information coming from other nanosensors, thus enabling a multi-hop transmission of information from a nanosensor to the nano-controller. In Sect. 2.1, we introduce the nanosensor deployment model, while in Sect. 2.2 we describe the main

steps of the multi-hop decision algorithm involving each nanosensor willing to transmit information and the nano-controller. In Sects. 2.3, 2.4, 2.5, and 2.6, the main elements of the routing framework, namely, the computation of the probability of energy saving and the CNR, and the management of the random back-off time and the optimal scheduling of the nanosensor transmissions in the sub-frames, are analytically detailed. The most frequently used parameters in this section are reported in Table 1 by following the order of their appearance in the text.

### 2.1 Nanosensor deployment

The nanosensors are assumed to be deployed in the 2-dimensional space occupied by a WNSN cluster according to a spatial homogeneous Poisson counting process whose rate is equal to the nanosensor density  $\rho$  defined in Table 1. For this, the probability of having a count of  $k$  nanosensors in an area of value  $S$  within the WNSN cluster is expressed as follows:

$$P(k \text{ nanosensors in } S) = \frac{[\rho S]^k e^{-\rho S}}{k!}. \quad (1)$$

### 2.2 Multi-hop decision algorithm

The multi-hop decision algorithm is executed in the wireless nanosensor network every time a nanosensor  $n$  is willing to transmit data. With reference to [18], the communication between nanosensors and the nano-controller follows a dynamic Time Division Multiple Access (TDMA) scheduling, where a time frame structure is divided into four fixed-length sub-frames: DownLink (DL), UpLink (UL), MultiHop (MH), and RandomAccess (RA). The DL sub-frame is used by the nano-controller to send commands to the nanosensors, the UL subframe is used by nanosensors to send data to the nano-controller by using transmission timeslots assigned by the nano-controller, the MH sub-frame is used by nanosensors to exchange data with each other in an ad-hoc fashion by using time slots assigned by the nano-controller, and the RA sub-frame is used for communication of the willingness to transmit data from nanosensors to the nano-controller.

The routing decision algorithm involves the following steps, as summarized through the block scheme in Fig. 1:

1. A nanosensor  $n$  sends to the nano-controller a request to transmit data, which specifies the amount of information it needs to transmit  $P_n$  defined in Table 1. This communication takes place in the RA subframe and it is directed only to the nano-controller.
2. Upon receiving the request to transmit data from a nanosensor  $n$ , the nano-controller estimates the distance  $z_n$  between itself and the nanosensor  $n$ , and from

**Table 1** Table of the most frequently used parameters in Sect. 2

Parameter	Definition
$\rho$	Nanosensor density in number of nanosensors per unit area
$P_n$	Amount of information the nanosensor $n$ needs to transmit in number of packets
$P_{ES}(n)$	Probability of energy savings by multi-hop transmission for the nanosensor $n$
$CNR_n$	Critical Neighborhood Range for the nanosensor $n$
$RTP_n$	Required Transmission Power for the nanosensor $n$
$T_{B-O}(n, k)$	Random back-off time for the nanosensor $k$ upon completion of the reception of the data transmission from the nanosensor $n$
$ACK(n, m)$	Acknowledgement for the nanosensor $k$ upon completion of the random back-off time $T_{B-O}(n, k)$
$E_{bit}(l)$	Energy per bit to transmit in a single hop at a distance $l$
$x_n$	Distance between the node $n$ and a random neighbor
$y_n$	Distance between the random neighbor of the nanosensor $n$ and the nano-controller
$z_n$	Distance between the node $n$ and the nano-controller
$\Phi$	Angle between the line connecting the nanosensor $n$ and the nano-controller and the line connecting the nanosensor $n$ and its random neighbor
$\hat{E}_{bit}(x_n, \Phi)$	Average energy per bit from the random neighbor of the nanosensor $n$ to the nano-controller
$S(z_n)$	Area spanned by all the possible values for the coordinates of a neighbor nanosensor in the plane defined by the angle between the line connecting the nanosensor $n$ and the nano-controller and the line connecting the nanosensor $n$ and the neighbor, which satisfy the inequality in (4)
$SNR$	Signal-to-Noise Ratio experienced by a receiver nanosensor
$P(l)$	Transmission power spent at a nanosensor to transmit in a single hop and guarantee a constant SNR at receiver placed at distance $l$
$C(l)$	Maximum data rate at which a nanosensor can transmit at a distance $l$ while guaranteeing a predefined received SNR value
$f_0$	
$c$	
$N_0$	
$E_r$	Energy spent at the nanosensor to receive one bit, which is a constant parameter within the scope of this paper
$\Lambda(l)$	Maximum data rate at which a nanosensor can transmit at a distance $l$ while guaranteeing a predefined received SNR value and infinite network lifetime
$\lambda_{harv}$	Energy harvesting rate for a nanosensor
$\lambda_{con}(l)$	Energy consumption rate for a nanosensor during transmission at a distance $l$
$D_n$	Size in bits of the incoming data from the nanosensor $n$
$e_m(t)$	Energy stored in the nanosensor $m$ at time $t$ is sufficient to complete the reception of the data from a nanosensor $n$
$RSSI(n, n - c)$	Received Signal Strength Indicator received at the nanosensor $n$ upon a transmission from the nano-controller $n - c$
$T_i$	Minimum transmission period per packet for each nanosensor
$N_{bits}$	Number of bits in a packet

the knowledge of the nanosensors density  $\rho$  it computes the value of the probability  $P_{ES}(n)$  of energy savings by multi-hop transmission for the nanosensor  $n$ , as explained in Sect. 2.3, through the expressions in (17), (19), and (6), respectively.

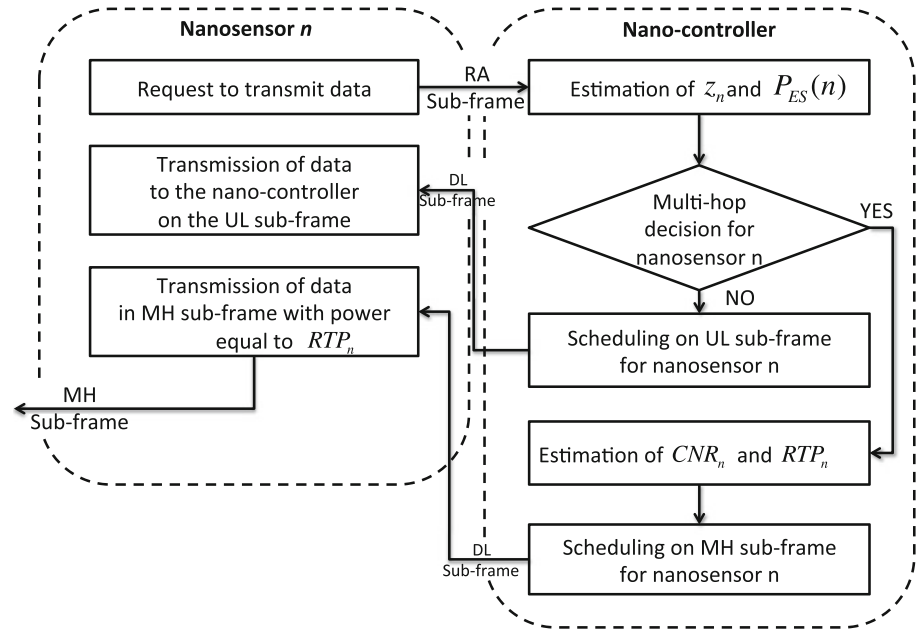
3. The nano-controller makes the decision for the nanosensor  $n$  to go either for a multi-hop transmission or for a single-hop transmission on the basis of the value of

the realization of a random variable with a Bernoulli distribution [12] having success probability equal to the probability  $P_{ES}(n)$  of energy savings. This is expressed as follows:

$$\Pr\{n \text{ Multi-hop}\} = 1 - \Pr\{n \text{ Single-hop}\} = P_{ES}(n), \quad (2)$$

4. In case of a single-hop transmission decision for the nanosensor  $n$ , the nano-controller performs a scheduling

**Fig. 1** Block Scheme of the multi-hop decision algorithm involving a nanosensor  $n$  and the nano-controller



on the UL sub-frame, as described in Sect. 2.6, where the nanosensor  $n$  is dynamically assigned variable-length time slots in the UL sub-frame on the basis of the communicated amount of information  $P_n$  it needs to transmit. The result of the scheduling is communicated from the nano-controller to the nanosensor  $n$  by using the DL sub-frame, and subsequently the data is transmitted directly from the nanosensor  $n$  to the nano-controller.

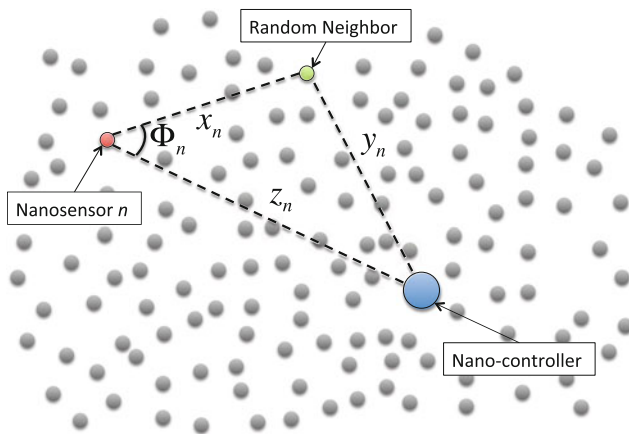
5. In case of multi-hop transmission decision for the nanosensor  $n$ , the following additional steps are performed:
  - The nano-controller computes for the nanosensor  $n$  the Critical Neighborhood Range  $CNR_n$ , which corresponds to the optimal distance at which the next hop should be located from the nanosensor  $n$  to achieve the best trade-off between the throughput and the distance from the receiving neighbor node that guarantees a predefined received SNR value, while at the same time satisfying the condition for infinite network lifetime. From the value of the  $CNR_n$ , the nano-controller computes the value of the Required Transmission Power  $RTP_n$  which the nanosensor  $n$  should use to achieve a predefined value for the received SNR at a receiver placed at a distance equal to  $CNR_n$ . The computations of  $CNR_n$  and  $RTP_n$  are detailed in Sect. 2.4 Moreover, the nano-controller, by applying the scheduling framework described in Sect. 2.6, assigns to the nanosensor  $n$  variable-length time slots within the MH sub-frame on the basis of the communicated amount of information  $P_n$  it needs to transmit, and communicates this information and the

value of the  $CNR_n$  to the nanosensor  $n$  by using the DL sub-frame.

- Upon reception of the information from the nano-controller transmitted in the DL sub-frame, the nanosensor  $n$  transmits its data in the MH sub-frame by using a transmission power equal to  $RTP_n$  and the time slots communicated by the nano-controller.
- Each nanosensor  $k$  receiving the data from the nanosensor  $n$ , upon completion of the reception of the data transmission, waits for a random back-off time  $T_{B-O}(n, k)$ . If a nanosensor  $m$  does not overhear in the RA sub-frame an Acknowledgement  $ACK(n, k)$  message, where  $k \neq m$ , then it broadcasts an  $ACK(n, m)$  in the RA sub-frame. The value of the back-off time  $T_{B-O}(n, k)$  whose computation is detailed in Sect. 2.5 allows the nanosensors which are located farther from the nanosensor  $n$ , but closer to the  $CNR_n$ , to be more likely selected as the next hop for the transmission of the data coming from the nanosensor  $n$ .
- Upon completion of the reception of the data coming from the nanosensor  $n$ , the wireless nanosensor network repeats the aforementioned steps from Step 1 this time for the next hop nanosensor  $m$ , which becomes the new source node.

### 2.3 Probability of energy savings by multi-hop transmission

The probability  $P_{ES}(n)$  of energy savings by multi-hop transmission for the nanosensor  $n$  is defined as the



**Fig. 2** Graphical representation of the nanosensor network for the computation of the probability of energy savings

probability of having a total average energy per bit consumption when adopting multi-hop transmission  $E_{b\text{-multi-hop}}(n)$  which is lower than the average energy per bit consumption  $E_{b\text{-direct}}(n)$  achieved with a direct path. This is expressed as follows:

$$P_{ES}(n) = \Pr\{E_{b\text{-multi-hop}}(n) \leq E_{b\text{-direct}}(n)\}. \quad (3)$$

The expression in (3) is translated into the probability of having at least one neighbor nanosensor, whose distance to the nano-controller is denoted as  $x_n$ , for which the energy per bit consumption when adopting multi-hop transmission is lower than the energy per bit consumption achieved with a direct path, as shown in Fig. 2. The energy per bit consumption when adopting multi-hop transmission with this neighbor nanosensor is equal to the sum of the energy per bit  $E_{bit}(x_n)$  to transmit at a distance  $x_n$ , the energy per bit  $E_{bit}(y_n)$  to transmit at a distance  $y_n$  between the neighbor and the nano-controller, and the energy  $E_r$  spent at the neighbor to receive one bit, which is a constant design parameter. The energy per bit consumption achieved with a direct path is equal to the energy per bit  $E_{bit}(z_n)$  to transmit at a distance  $z_n$  between the nanosensor  $n$  and the nano-controller. As a consequence, the expression in (3) becomes

$$P_{ES}(n) = \Pr\{\exists(x_n, y_n) : E_{bit}(x_n) + E_{bit}(y_n) + E_r \leq E_{bit}(z_n)\}, \quad (4)$$

where  $x_n$  and  $y_n$  are the distance between the neighbor nanosensor and the nanosensor  $n$ , and the distance between the neighbor nanosensor and the nano-controller, respectively, as shown in Fig. 2.  $\exists$  denotes the existence of a node whose distances  $x_n$  and  $y_n$  satisfy the inequality in (4).  $z_n$  is the distance between the nano sensor  $n$  and the nano-controller, which is a known parameter to the nano-controller for each nanosensor  $n$ .

The probability  $P_{ES}(n)$  of energy savings by multi-hop transmission for the nanosensor  $n$  is a function of the density  $\rho$  of nanosensors and the distance  $z_n$  between the nanosensor  $n$  and the nano-controller, while the distance  $x_n$  between the nano sensor  $n$  and a random neighbor and the distance  $y_n$  between the neighbor and the nano-controller are considered random variables which depend on a spatial Poisson counting process [12] whose rate is equal to the density  $\rho$  of nanosensors. As a consequence, the expression in (4) is equivalent to one minus the probability in aforementioned spatial Poisson process of having a count equal to zero in the area  $S(z_n)$ , derived from (1), and it is expressed as follows:

$$P_{ES}(n) = 1 - e^{-\rho S(z_n)}, \quad (5)$$

where  $S(z_n)$  is defined as the area spanned by all the possible values for the coordinates of a neighbor nanosensor in the plane defined by  $x_n \in [0, \infty]$  and  $\Phi \in [0, 2\pi]$ , which is the angle between the line connecting the nanosensor  $n$  and the nano-controller and the line connecting the nanosensor  $n$  and the neighbor, as shown in Fig. 2 which satisfy the inequality in (4). The area  $S(z_n)$  is therefore computed through the following expression:

$$S(z_n) = \iint_{\{(x_n, \Phi) | E_{bit}(x_n) + \hat{E}_{bit}(x_n, \Phi) \leq E_{bit}(z_n) - E_r\}} x dx d\phi. \quad (6)$$

where  $E_{bit}(x_n)$ ,  $E_{bit}(z_n)$ , and  $\hat{E}_{bit}(x_n, \Phi)$  are the average energy per bit to transmit at a distance  $x_n$ ,  $z_n$ , and from the neighbor nanosensor to the nano-controller, respectively, and guarantee a constant Signal-to-Noise Ratio SNR at a receiver. In the following, we detail the formulas for these parameters necessary to evaluate (6).

The average energy per bit  $E_{bit}(l)$  to transmit at a distance  $l$  is defined as the ratio between the transmission power  $P(l)$  spent at a nanosensor and the maximum transmission bit-rate  $C(l)$ , both functions of the distance  $l$  between the transmitting nanosensor and the receiver, which can be either another nanosensor or the nano-controller. This is expressed as follows:

$$E_{bit}(l) = \frac{P(l)}{C(l)}. \quad (7)$$

The transmission power  $P(l)$  spent at a nanosensor as a function of the distance  $l$  is defined as the power necessary in transmission to guarantee a constant Signal-to-Noise Ratio SNR at a receiver placed at a distance  $l$  from the transmitting nanosensor. This is expressed as

$$P(l) = \int_{B_{3dB}(l)} \text{SNRA}(l, f) S_N(l, f) df, \quad (8)$$

where  $A(l, f)$  and  $S_N(l, f)$  are the total path loss and the total molecular absorption noise Power Spectral Density

(PSD) as a function of the distance  $l$  and the frequency  $f$ , and  $B_{3dB}(l)$  is the 3dB bandwidth as a function of the distance  $l$  [8]. The total path loss  $A(l, f)$  is computed through the following expression:

$$A(l, f) = \left(\frac{4\pi f_0 l}{c}\right)^2 e^{k(f)l}, \tag{9}$$

where  $c$  is the speed of light in the vacuum,  $k(f)$  is the molecular absorption coefficient as a function of the frequency  $f$ , and  $f_0$  is the design center frequency [18]. The total molecular absorption noise PSD  $S_N$  is contributed by the atmospheric noise  $S_{N_0}$  [2] and the induced noise  $S_{N_1}$ , and can be obtained as

$$S_N(l, f) = S_{N_0}(l, f) + S_{N_1}(l, f), \tag{10}$$

$$S_{N_0}(l, f) = \lim_{l \rightarrow \infty} k_B T_0 (1 - \exp(-k(f)l)) \left(\frac{c}{\sqrt{4\pi f_0}}\right)^2, \tag{11}$$

$$S_{N_1}(l, f) = S(f)(1 - \exp(-k(f)l)) \left(\frac{c}{4\pi f_0}\right)^2, \tag{12}$$

where  $l$  refers to the transmission distance,  $f$  stands for the frequency,  $k_B$  is the Boltzmann constant,  $T_0$  is the room temperature,  $k$  is the molecular absorption coefficient,  $c$  is the speed of light in the vacuum,  $f_0$  is the design center frequency, and  $S$  is the PSD of the transmitted signal. In this paper, we consider the following assumption:

- The frequency range defined by the 3dB bandwidth  $B_{3dB}(l)$  as a function of the distance  $l$  is not affected by molecular absorption. This is expressed as follows:

$$k(f)|_{f \in B_{3dB}(l)} \approx 0, \tag{13}$$

As a consequence, the expressions of the total path loss and the total molecular absorption noise are simplified as follows:

$$A(l, f) = A(l) = \left(\frac{4\pi f_0 l}{c}\right)^2, \tag{14}$$

where  $l$  and  $f_0$  are the distance and the design center frequency, respectively, and  $c$  is the speed of light in the vacuum;

$$S_N(l, f) = N_0, \tag{15}$$

where  $N_0$  is a constant.

By taking into account that the transmission power  $P(l)$  expressed in (8) guarantees a constant SNR at a receiver placed at a distance  $l$  from the transmitting nanosensor, the maximum transmission bit-rate  $C(l)$  as a function of the distance  $l$  is expressed as follows:

$$C(l) = \int_{B_{3dB}(l)} \log_2(1 + \text{SNR}) df = B_{3dB}(l) \log_2(1 + \text{SNR}), \tag{16}$$

where  $B_{3dB}(l)$  is the 3dB bandwidth as a function of the distance  $l$  [18].

The average energy per bit  $E_{bit}(l)$  to transmit at a distance  $l$  is computed from (7), (8), (14), and (15), and (16), and it results in the following expression

$$E_{bit}(l) = \left(\frac{4\pi f_0}{c}\right)^2 \frac{N_0 \text{SNR}}{\log_2(1 + \text{SNR})} l^2, \tag{17}$$

where  $N_0$  is a constant,  $l$  is the distance,  $f_0$  is the design center frequency,  $c$  is the speed of light in the vacuum, and SNR is the constant signal-to-noise ratio guaranteed at the receiver.

The average energy per bit  $\hat{E}_{bit}(x_n, \Phi)$  from the neighbor nanosensor to the nano-controller is computed by taking into account that the random variable  $y_n$  is a function of two independent random variables  $x_n$  and  $\Phi$ , the distance between the nanosensor  $n$  and a neighbor, and the angle between the line that connects the nanosensor  $n$  with the nano-controller and the line that connects the nanosensor  $n$  with the neighbor, as shown in Fig. 2, through the law of cosines, expressed as

$$y_n = \sqrt{x_n^2 + z_n^2 - 2x_n z_n \cos \Phi}, \tag{18}$$

where  $z_n$  is the distance between the nanosensor  $n$  and the nano-controller,  $x_n$  is the distance between the nanosensor  $n$  and a random neighbor,  $y_n$  is the distance between the neighbor and the nano-controller, and  $\Phi$  is the angle between the line connecting the nanosensor  $n$  and the nano-controller and the line connecting the nanosensor  $n$  and the neighbor. As a consequence,  $\hat{E}_{bit}(x_n, \Phi)$  is expressed through the substitution of (18) into (17) as

$$\hat{E}_{bit}(x_n, \Phi) = \left(\frac{4\pi f_0}{c}\right)^2 \frac{N_0 \text{SNR}}{\log_2(1 + \text{SNR})} (x_n^2 + z_n^2 - 2x_n z_n \cos \Phi), \tag{19}$$

#### 2.4 Critical neighborhood range for throughput-distance trade-off and infinite network lifetime

The Critical Neighborhood Range  $CNR$  is computed by investigating a trade-off for a nanosensor between the throughput and the distance from the receiving neighbor node that guarantees a predefined received SNR value, while at the same time satisfying the condition for infinite network lifetime.

The throughput  $\Lambda(l)$  is defined as the maximum data rate at which a nanosensor can transmit at a distance  $l$  while guaranteeing a predefined received SNR value and infinite network lifetime. This is expressed as

$$\Lambda(l) = C(l) \lambda^c(l), \tag{20}$$

where  $C(l)$  is the maximum transmission bit-rate as a function of the distance  $l$ , and  $\lambda^c(l)$  is the Critical Transmission Ratio (CTR) given in [18], and defined as

the ratio between the energy harvesting rate  $\lambda_{harv}$  and the energy consumption rate  $\lambda_{con}(l)$  for a nanosensor during transmission, expressed as

$$\lambda^c(l) = \frac{\lambda_{harv}}{\lambda_{con}(l)}, \tag{21}$$

where the energy harvesting rate  $\lambda_{harv}$ , when the nanosensors are provided by piezoelectric nano-generators to harvest vibrational energy [19], has the following expression [18]:

$$\lambda_{harv} = \frac{1}{2} C_{cap} V_g^2 \left( 2 \frac{\Delta Q}{V_g C_{cap}} \exp\left(-\frac{\Delta Q}{V_g C_{cap}} n_{cycle}\right) - 2 \frac{\Delta Q}{V_g C_{cap}} \exp\left(-2 \frac{\Delta Q}{V_g C_{cap}} n_{cycle}\right) \right), \tag{22}$$

where  $V_g$  is the generator voltage,  $C_{cap}$  refers to the ultra-nano-capacitor capacitance,  $\Delta Q$  is the electric charge harvested per cycle, and  $n_{cycle}$  is the rate of the vibrational energy source. The energy consumption rate  $\lambda_{con}(l)$  is computed as the product between the maximum transmission bit-rate  $C(l)$  and the average energy per bit  $E_{bit}(l)$  to transmit at a distance  $l$ , expressed in (17), as

$$\lambda_{con}(l) = C(l)E_{bit}(l), \tag{23}$$

As a consequence, the throughput  $\Lambda(l)$  that guarantees a predefined received SNR value and infinite network lifetime can be expressed after substituting (23) into (21) and (20) as

$$\Lambda(l) = \frac{\lambda_{harv}}{E_{bit}(l)}, \tag{24}$$

The  $CNR_n$  is defined as the distance between the nanosensor  $n$  and a potential neighbor for which the throughput  $\Lambda(CNR_n)$  from the nanosensor  $n$  to the neighbor is on average equal to the throughput  $\Lambda(y_n)$  from the neighbor to the nano-controller, where  $y_n$  is the distance

between the neighbor and the nano-controller. It is necessary to guarantee that the next hop neighbor is placed as close as possible to  $CNR_n$  in order to maximize the next hope distance range while at the same time achieving the highest possible throughput from the nanosensor  $n$  to the nano-controller. The  $CNR_n$  is computed through the following equation, whose main parameters are graphically represented in Fig. 3:

$$CNR_n = \left\{ x_n | x_n = \frac{\int_{(x_n, \Phi)} \sqrt{(z_n - x_n \cos \Phi)^2 + (x_n \sin \Phi)^2} d\Phi}{\int_{(x_n, \Phi)} d\Phi} \right\}, \tag{25}$$

subject to:

$$(x_n, \Phi) \in \{(x_n, \Phi) | E_{bit}(x_n) + \hat{E}_{bit}(x_n, \Phi) \leq E_{bit}(z_n) - E_r\}, \tag{26}$$

where the throughput  $\Lambda(l)$  is computed through the expression in (24), (17), and (22), while  $x_n$  is the distance between the nanosensor  $n$  and a neighbor,  $\Phi$  the angle between the line that connects the nanosensor  $n$  with the nano-controller and the line that connects the nanosensor  $n$  with the neighbor,  $z_n$  is the distance between the nanosensor  $n$  and the nano-controller,  $E_{bit}(x_n)$  and  $\hat{E}_{bit}(x_n, \Phi)$  are expressed in (17) and (19), respectively, and  $E_r$  is the energy spent at the neighbor to receive one bit, which is constant design parameter.

Finally, the nano-controller computes the  $RTP_n$  as the power that the nanosensor  $n$  should use to achieve a predefined value for the received SNR at a receiver placed at a distance equal to  $CNR_n$ . The  $RTP_n$  is computed through the following expression:

$$RTP_n = \int_{B_{3dB}(CNR_n)} SNRA(CNR_n, f) S_N(CNR_n, f) df, \tag{27}$$

where  $A(l, f)$  and  $S_N(l, f)$  are the total path loss and the total molecular absorption noise PSD computed for a value of the distance equal to  $CNR_n$ , and as a function of the frequency  $f$ , respectively, and  $B_{3dB}(CNR_n)$  is the 3dB bandwidth for a distance  $CNR_n$  [18]. The total path loss  $A(CNR_n, f)$  at a distance  $CNR_n$  is computed through the expression in (9), while the noise PSD  $S_N(CNR_n, f)$  is given by (15).

### 2.5 Random back-off time for node load fairness

The availability to be the next hop for the nanosensor  $n$  is decided by a nanosensor  $m$  at time instant  $t$  upon starting the reception of the incoming data  $D_n$  from the nanosensor  $n$  transmitted in selected time slots of the MH sub-frame, as expressed through the block scheme in Fig. 4. The nanosensor

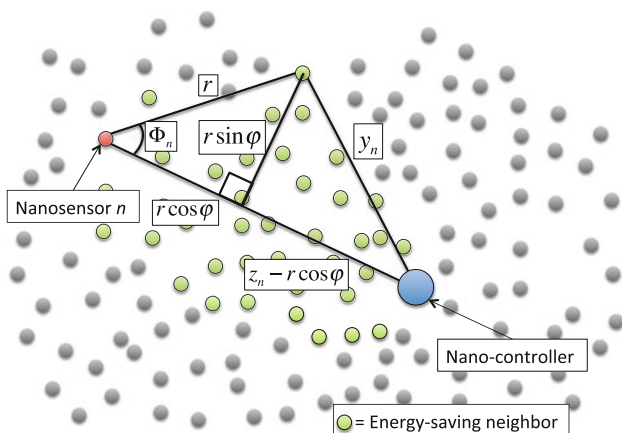
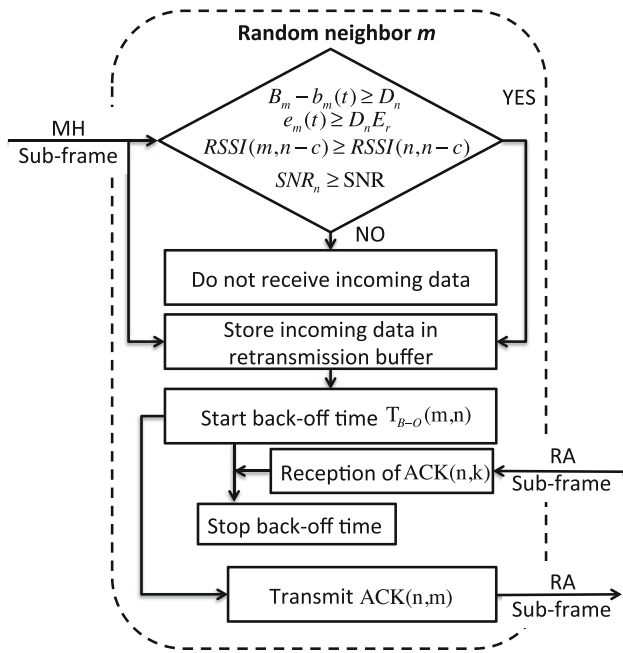


Fig. 3 Graphical representation of the main parameters involved in the computation of the CNR





**Fig. 4** Block Scheme of the algorithm executed at a random neighbor upon the reception of data from the nanosensor  $n$  in the MH sub-frame

$m$  stores the received data in the retransmission buffer, sets the random back-off time  $T_{B-O}(m)$ , and it is available to be the next hop only if all the following conditions are met:

- There is enough room in the retransmission buffer of the nanosensor  $m$  to store the data received from the nanosensor  $n$ . This is expressed as follows:

$$B_m - b_m(t) \geq D_n, \tag{28}$$

where  $B_m$  is the total size in bits of the retransmission buffer of the nanosensor  $m$ ,  $b_m(t)$  is the size in bits of the data stored in the retransmission buffer of the nanosensor  $m$  at time  $t$ , and  $D_n$  is the size in bits of the incoming data from the nanosensor  $n$ , which is communicated to the nanosensor  $m$  by the nanosensor  $n$  at the beginning of the transmission.

- The energy  $e_m(t)$  stored in the nanosensor  $m$  at time  $t$  is sufficient to complete the reception of the data from the nanosensor  $n$ . This is expressed as follows:

$$e_m(t) \geq D_n E_r, \tag{29}$$

where  $D_n$  is the size in bits of the incoming data from the nanosensor  $n$ , and  $E_r$  is the energy spent to receive one bit.

- The Signal-to-Noise Ratio  $SNR_n$  of the reception at the nanosensor  $m$  from the nanosensor  $n$  is higher than the constant SNR value guaranteed at the receiver defined in Sect. 2.2 This is expressed as

$$SNR_n \geq SNR, \tag{30}$$

- The nanosensor  $m$  is closer to the nano-controller than the nanosensor  $n$ . This translates into a condition based on

the Received Signal Strength Indicator (RSSI), which is a measurement proportional to the power received at a nanosensor. The condition states that the  $RSSI(m, n - c)$  received at the nanosensor  $m$  upon a transmission from the nano-controller  $n - c$ , measured by the nanosensor  $m$  during any DL sub-frame, should be higher than the  $RSSI(n, n - c)$  received at the nanosensor  $n$  upon a transmission from the nano-controller  $n - c$ , measured by the nanosensor  $n$  during any DL subframe and communicated to the nanosensor  $m$  before starting the transmission of the data in the MH sub-frame. This condition is expressed as follows:

$$RSSI(m, n - c) \geq RSSI(n, n - c), \tag{31}$$

If the aforementioned conditions are met, the nanosensor  $m$  stores in the retransmission buffer the data received from the nanosensor  $n$ , and starts the back-off time  $T_{B-O}(m, n)$  upon the end of the data reception. The value of the back-off time  $T_{B-O}(m, n)$  is a realization of an exponential distribution [12] expressed as follows:

$$f_{T_{B-O}(m,n)}(t) = \frac{e^{-\frac{t}{\hat{T}_{B-O}(m,n)}}}{\hat{T}_{B-O}(m,n)}, \tag{32}$$

where  $\hat{T}_{B-O}(m, n)$  is the average value of the back-off time for the nanosensor  $m$  upon reception of data from the nanosensor  $n$ , and it is proportional to the  $RSSI(m, n)$  received at the nanosensor  $m$  upon a transmission from the nanosensor  $n$ , expressed as follows:

$$\hat{T}_{B-O}(m, n) = K_{B-O} RSSI(m, n), \tag{33}$$

where  $K_{B-O}$  is a constant system design parameter. On the one hand, if during the back-off time the nanosensor  $m$  overhears an Acknowledgement  $ACK(n, k)$  message in the RA sub-frame, where  $k \neq m$ , it stops the back-off time and deletes from the retransmission buffer the data received from the nanosensor  $n$ . On the other hand, upon timeout of the back-off time  $T_{B-O}(m, n)$ , the nanosensor  $m$  broadcasts an  $ACK(n, m)$  in the RA sub-frame. The expression in (33) allows the nanosensors which are located farther from the nanosensor  $n$ , but closer to the CNR defined in Sect. 2.4, to have a shorter average back-off time than the other nanosensors, and consequently to be more likely selected as the next hop for the transmission of the data coming from the nanosensor  $n$ .

## 2.6 Optimal scheduling of the up link and multi hop sub-frames

### 2.6.1 Up link sub-frame scheduling

The UL sub-frame scheduling algorithm is required to schedule the transmissions of nanosensors which use direct/single-hop communications with the nano-controller.

In this case, based on Theorem 2 in [18], the nanosensors can be divided into two groups: **near-region sensors** and **far-region sensors**. The near-region sensors, which are within a distance  $D$  from the nano-controller, always have their energy harvesting rate  $\lambda_{harv}$  larger than their energy consumption rate  $\lambda_{con}(l)$ . This means that the maximum single-user throughput  $\Lambda^{near}(l)$  of a near-region sensor can approach its maximum achievable data rate  $C(l)$  defined in (16) as follows:

$$\Lambda^{near}(l) = C(l), \forall l < D. \quad (34)$$

In contrast to the near-region sensors, the far-region sensors, which are at least  $D$  far away from the nano-controller, always have their energy harvesting rate  $\lambda_{harv}$  less than their energy consumption rate  $\lambda_{con}(l)$ . Therefore, the far-region sensors always need to enter the sleep state for recharging before their next packet transmissions. This implies that the far-region sensors have the maximum single-user throughput  $\Lambda^{far}(l)$  necessarily smaller than the maximum achievable data rate  $C(l)$ . This indicates the unbalanced transmission rates between near-region sensors and far-region sensors. Specifically, we have the following expression:

$$\Lambda^{far}(l) = \lambda^c(l)C(l), \forall l \geq D, \quad (35)$$

where CTR  $\lambda^c(l)$  is always less than 1.

Based on the above observations, we adopt a similar scheduling as in [18], which decides on the packet transmission order of the nanosensors with the objective to guarantee the infinite network lifetime with balanced single-user throughput between far-region nanosensors and near-region nanosensors. The proposed scheduling algorithm involves the following steps.

*Step 1:* Calculate the minimum transmission period (MTP) per packet  $T_i$  for each nanosensor. Specifically, a near-region nanosensor has the following MTP:

$$T_i = N_{bits}/\Lambda^{near}(l_i), \quad (36)$$

and a far-region nanosensor has the following MTP:

$$T_i = N_{bits}/\Lambda^{far}(l_i). \quad (37)$$

Next, set the initial schedule length  $L^\Gamma = \max_{i \leq M} T_i$ , where  $M$  is the total number of nanosensors within the cluster. Let  $l_{max} = \max_{i \leq M} l_i$ . This results in

$$L^\Gamma = N_{bits}/\Lambda^{far}(l_{max}). \quad (38)$$

*Step 2:* Associate each nanosensor  $n_i$  with a schedule  $S_i$ . Set the packet counter in  $S_i$  as  $N_i^\Gamma = 0$ . Then, calculate the packet transmission time as follows:

$$T_i^{pk} = N_{bits}/R_{opt}(l_i) \quad (39)$$

for each nanosensor  $n_i$ . Next, arrange the nanosensors  $\{n_i\}_{i \leq M}$  in the order of increasing maximum single-user

throughput  $\Lambda$ . Assign each nanosensor a priority  $p_i = i$ , i.e., the nanosensor with smaller  $\Lambda$  has higher priority.

*Step 3:* At the initial schedule decision time  $\tau = 0$ , the nanosensor  $n_i$  is scheduled to transmit at  $\tau$  if the following three conditions are satisfied. (1) It has the highest priority. (2) The *backward difference* between the current time  $\tau$  and the start time of  $n_i$ 's previous packet is not smaller than its MTP per packet  $T_i$ , i.e.,

$$\tau - s_{i,N_i^\Gamma} \geq T_i. \quad (40)$$

(3) The *forward difference* between the current time  $\tau$  and  $n_i$ 's first packet transmission time is not smaller than its MTP per packet  $T_i$ . This is expressed as follows:

$$L^\Gamma - \tau + s_{i,1} \geq T_i. \quad (41)$$

If  $n_i$  is scheduled to transmit at time  $\tau$ , the next schedule decision time follows  $\tau = \tau + T_i^{pk}$ .

**Step 4:** Repeat Step 3 until every nanosensor  $i$  is done sending the total amount of  $P_i$  packets, which is specified by a nanosensor  $i$  when it sends the request message to the nano-controller.

## 2.6.2 Multi-hop sub-frame scheduling

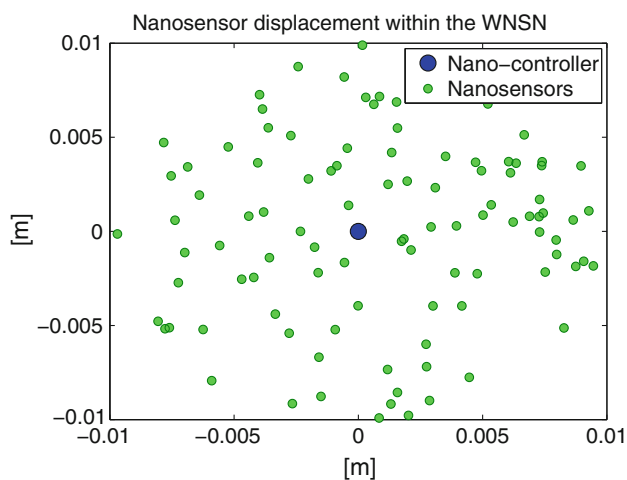
The MH sub-frame scheduling aims to schedule the transmission order for the nanosensors for which the nano-controller decided for a multi-hop transmission. We adopt the same scheduling algorithm as for the UL sub-frame case by redefining the near-region nanosensors and far-region nanosensors. More specifically, we define  $l_{ij}$  as the distance between a nanosensor  $i$  and relay node  $j$ . Then, the near-region nanosensors are characterized by a distance  $l_{ij}$  less than the critical distance  $D^c$ , defined as the distance that satisfies  $\lambda_{D^c} = 1$ . The far-region nanosensors are characterized by a distance  $l_{ij}$  larger than the critical distance  $D^c$ . Then, the maximum single-user throughput of the near-region and far-region nanosensors is computed through (34) and (35). Then, the scheduling algorithm as described for the UL sub-frame case is applied.

## 3 Numerical results

In this Section, we evaluate the performance of the proposed framework by means of extensive network simulations and discuss the results in detail. In Sect. 3.1, we describe the simulation setup and the applied parameter values, while in Sect. 3.2 we present the numerical results of the main quantities involved in the routing framework. Finally, in Sect. 3.2 we present an evaluation of the proposed routing framework against single-hop communication in terms of energy savings, capacity, and delay.

### 3.1 Simulation setup

In our simulation, we use the following parameter values. As shown in Fig. 5, the nanosensors are deployed according to a spatial homogeneous Poisson process as described in Sect. 2.1, where the density  $\rho$  has a value corresponding to a count of 100 nanosensors within an area  $S$  equal to a circle with radius 10 mm. The Terahertz Band channel is modeled as in [8], for a standard gaseous medium with 10% of water vapor molecules. The size of a packet is set to 256 bits, while the predefined value for the received SNR, on the basis of which we based the computation of the probability of energy savings in Sect. 2.3, the critical neighborhood range in Sect. 2.4, and the random neighbor algorithm in Sect. 2.5, is set to 10. The piezoelectric energy harvesting system has the following parameters. We consider a capacitor with  $C_{cap} = 9\text{nF}$  charged at  $V_g = 0.42\text{V}$  for the computation of the energy  $e_m(t)$  stored in the nanosensor  $m$  at time  $t$  used in (29). For the computation of the energy harvesting rate  $\lambda_{harv}$  in (22), an ambient vibration with an average time between vibrations  $t_{cycle} = 1/50\text{s}$  is considered. The amount of charge  $\Delta Q$  harvested per cycle is 6 pC. The battery is fully discharged at the beginning of a simulation. The value of the energy  $E_r$  spent at a neighbor to receive one bit is set to 1/10 of the energy  $E_{bit}(l)$  expressed in (17) required to transmit a bit at a distance  $l$  equal to 1 mm. The simulation of the whole WNSN is iterated 100 times, where each iteration accounts for different realizations of the stochastic process of the nano-controller decision for each nanosensor to go either for a multi-hop transmission or for a single-hop transmission, expressed in (2). The results in terms of energy, capacity and delay, presented in Sect. 3.3, are computed by averaging the values resulting from all the iterations. For



**Fig. 5** Plot of the coordinates of 100 nanosensors deployed according to a homogeneous spatial Poisson process within a circle of radius 10 mm

computational reasons, the simulations of the multi-hop transmissions account only for a maximum of two hops between the source nanosensor and the nano-controller. As confirmed by the results presented in the following, this does not prevent from evaluating the overall benefits of having a multi-hop transmission in a WNSN.

### 3.2 WNSN routing framework

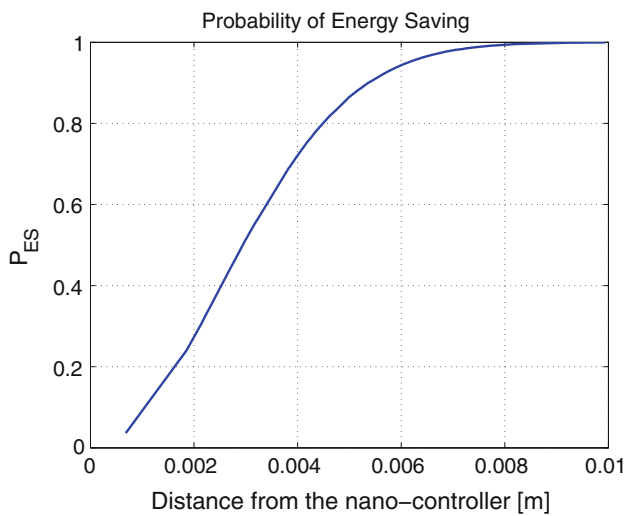
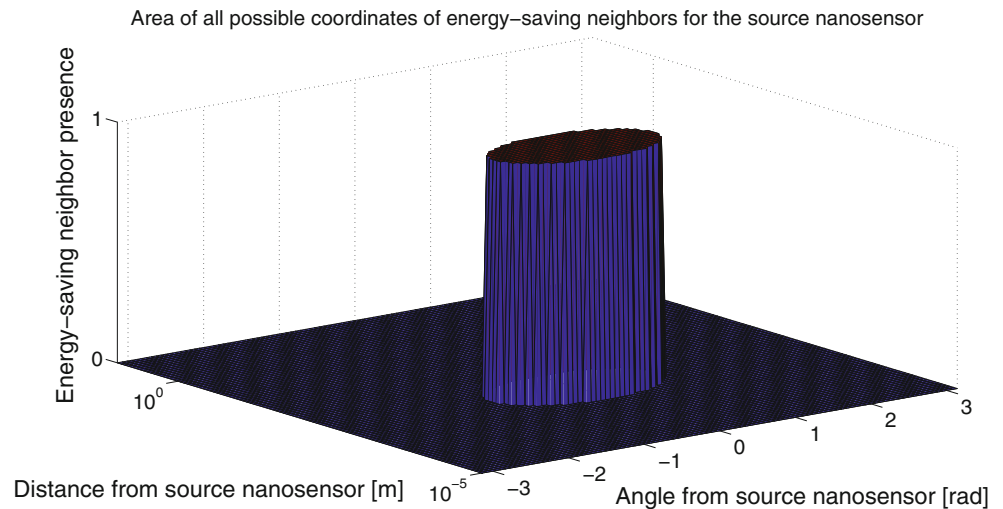
Numerical results for the area  $S(z_n)$  defined as the area spanned by all the possible values for the coordinates of an energy-saving neighbor nanosensor in the plane defined by the distance and the angle from the source nanosensor are shown in Fig. 6, where the distance is limited between 0 and 10 mm, while the angle is limited between 0 and  $2\pi$  rad. The area  $S(z_n)$  is restricted to a region between  $-1.047$  rad and  $1.047$  rad, and at a distance from the source nanosensor between 0.1 and 0.5 mm. This behavior is induced by the fact that the  $E_r$  spent at a neighbor to receive one bit is a constant value for all the possible neighbor nodes, and therefore is a constant term in the inequality in (4). As a consequence, the probability of energy savings is very low for both neighbors located too close to the source nanosensor, e.g., at less than 0.1 mm, and neighbors located too far from the source nanosensor, e.g., at more than 0.5 mm. The restriction of the area  $S(z_n)$  within a limited range of angles is given by the fact that the energy savings have high values only for a neighbor located reasonably between the source nanosensor and the nano-controller. Any other neighbor would deviate the route of the packets from the source nanosensors too far away from the nano-controller.

Values for the probability  $P_{ES}(n)$  of energy savings by multi-hop transmission are shown in Fig. 7, plotted for a distance of the source nanosensor from the nano-controller between 0.01 and 10 mm. As expected, the probability of energy savings has a low value for short distances, while it monotonically increases with the distance until reaching a value close to 1 for a distance longer than 8 mm. Clearly, as the distance of the source nanosensor from the nano-controller increases, the benefits of a multi-hop transmission in terms of energy saving become more and more evident.

### 3.3 Performance evaluation

The numerical values of the energy spent per nanosensor to transmit all its packets to the nano-controller is shown in Fig. 8, where the case of multi-hop routing, proposed in this paper, is compared to the case of single-hop communication. For short distances between a source nanosensor and the nano-controller, the energy spent is comparable, while as the distance gets longer, the energy saved through the multi-hop routing becomes higher and higher in agreement with the values of the probability of energy

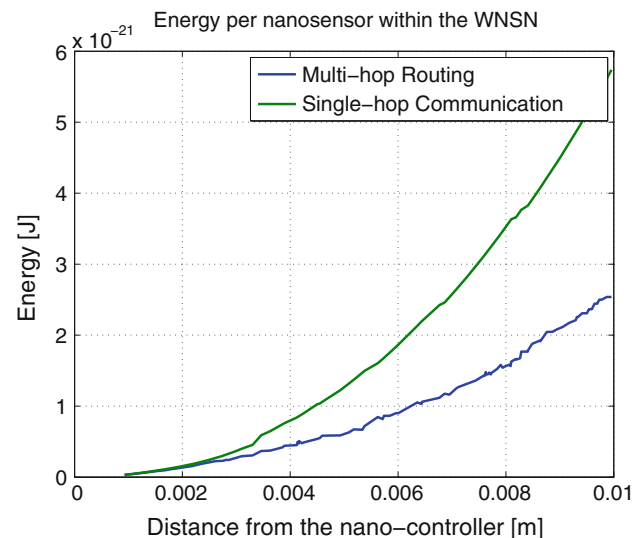
**Fig. 6** Area spanned by all the possible values for the coordinates of a neighbor nanosensor when the probability of energy saving is over a threshold



**Fig. 7** Probability of energy saving by multi-hop for a distance between the source nanosensor and the nano-controller between 0.01 and 10 mm

savings shown in Fig. 7. These results confirm the benefits in terms of energy that can derive from the adoption of the proposed multi-hop routing framework in a WNSN.

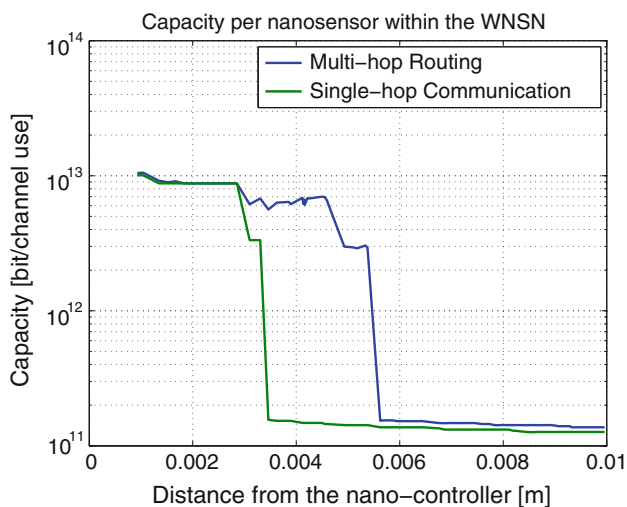
The numerical results in terms of capacity in bits per channel use experienced by nanosensors at different distances from the nano-controller are shown in Fig. 9. At distances shorter than 0.3 mm, the capacity has the same value for both the cases, since the probability of energy saving by multi-hop, and consequently the probability of a multi-hop decision from the nano-controller, is very low. For a distance between 0.3 and 0.56 mm, the multi-hop transmission shows higher values for the capacity, while for a distance higher than 0.56 mm the benefits of the multi-hop transmission on the capacity are less evident. This behavior can be explained by the fact that in this simulation we account for a maximum of two hops between each source



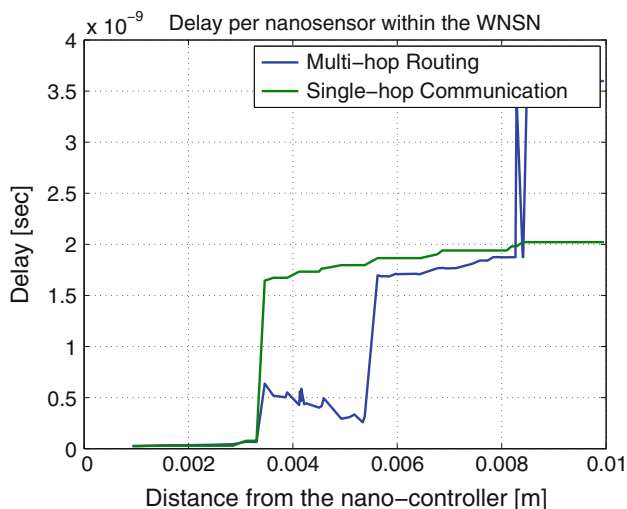
**Fig. 8** Comparison between the energy spent per nanosensor for the case of multi-hop routing and for the case of single-hop communication. Each nanosensor is characterized by its distance from the nano-controller, ranging from 0.01 to 10 mm

nanosensor and the nano-controller. For this, we limit the number of hops even for a distance that would require a hop number, thus limiting the reachable capacity to a value comparable to the single-hop communication case.

Finally, the numerical results in terms of delay experienced by the packets transmitted by each source nanosensor to reach the nano-controller are shown in Fig. 10. For a distance between the source nanosensor and the nano-controller lower than 0.3 mm the delay has the same values for both the cases, since, as mentioned above, the probability of a multi-hop decision from the nano-controller is very low. For a distance between 0.3 and 0.82 mm, the multi-hop transmission is characterized by an overall lower delay if compared to the single-hop communication. This is



**Fig. 9** Comparison between the capacity per nanosensor for the case of multi-hop routing and for the case of single-hop communication. Each nanosensor is characterized by its distance from the nano-controller, ranging from 0.01 to 10 mm



**Fig. 10** Comparison between the delay per nanosensor for the case of multi-hop routing and for the case of single-hop communication. Each nanosensor is characterized by its distance from the nano-controller, ranging from 0.01 to 10 mm

explained by the increased throughput of the nanosensors when transmitting over shorter distances, to a neighbor, as opposed to a direct transmission to the nano-controller. Unfortunately, as the distance increases over 0.82 mm, the delay of the multi-hop transmission assumes much higher values than the values for the single-hop communication. This can be again explained by the fact that in this simulation we account for a maximum of two hops between each source nanosensor and the nano-controller. As a consequence, over 0.82 mm the benefits of a shorter transmission distance given by the multi-hop transmission are overtaken by the increased delay in the reception and

retransmission of packets at the next-hop neighbors with respect to the single-hop communication.

## 4 Conclusions

In this paper, we have proposed a routing framework for Wireless NanoSensor Networks (WNSNs) which takes into account the two main characteristics of the nanosensors, namely, their Terahertz Band wireless communication and their nanoscale energy harvesting process. Solutions from the literature, focused on energy-efficient routing Wireless Sensor Networks (WSN) with energy harvesting capabilities, are not directly applicable to WNSNs, since the peculiarities of the Terahertz Band communication, in particular the very unique distance-dependent behavior of the available bandwidth and the power control techniques that can be employed to reach the optimal transmission rate, are not taken into account. Moreover, other work focused on routing in WSN with energy harvesting nodes does not capture the particular characteristics of the energy harvesting processes at the nanoscale, in particular the collection of vibrational energy through piezoelectric nanogenerators. Based on the aforementioned nanosensor characteristics, combined with the nanosensors limitation in terms of computational resources, and the need to efficiently meet the conditions for perpetual network operations, the routing framework detailed in this paper is specifically designed to save the average energy harvested from the environment by the nanosensors, and at the same time increase the overall throughput in the transmission of information from the nanosensors to the nano-controller.

The routing framework proposed in this paper is designed on top of a previously proposed MAC protocol for the joint throughput and lifetime optimization in WNSNs, and it uses a hierarchical cluster-based architecture that pushes the network operation complexity towards the cluster heads, or nano-controllers. Moreover, this routing framework is based on the evaluation of the probability of saving energy through a multi-hop transmission, the tuning of the transmission power of each nanosensor for throughput and hop distance optimization, and the selection of the next hop nanosensor on the basis of their available energy and current load.

Numerical results are presented for the main quantities involved in the proposed routing framework, such as the probability of energy saving by performing multi-hop transmission from a source nanosensor as a function of its distance from the nano-controller. A performance evaluation of the proposed multi-hop routing framework is conducted through simulations, where key parameters such as the energy savings, the capacity, and the delay experienced by each nanosensor of the WNSN demonstrate the figures

of merit of the proposed framework over a more basic single-hop communication.

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